

Fractal Aggregate Formation
Of Aerosols

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Presentation Overview

Review: What is an aerosol? What is a fractal?

Size and growth of aggregating particles

Aerosol to aerogel

Estimating size of aggregates with fractal math

Ball Lightning

- Oxidation of particles in air

- Electric field effects

- Soil aggregates in air

- Spectral analysis

Defining Aerosols

An aerosol is a suspension of fine particles (1-10nm) in a gaseous media.

- i. Can be described as in terms of concentration
- ii. Particles can exist outside of suspension for long periods of time

Aerosol	Not an Aerosol
A cloud of superfine dust	A flock of birds
Campfire smoke	Clouds

Aerosols are termed based on their origin

- i. Primary aerosols – product of a chemical reaction
- ii. Secondary aerosols – product of gas-to-particle conversion

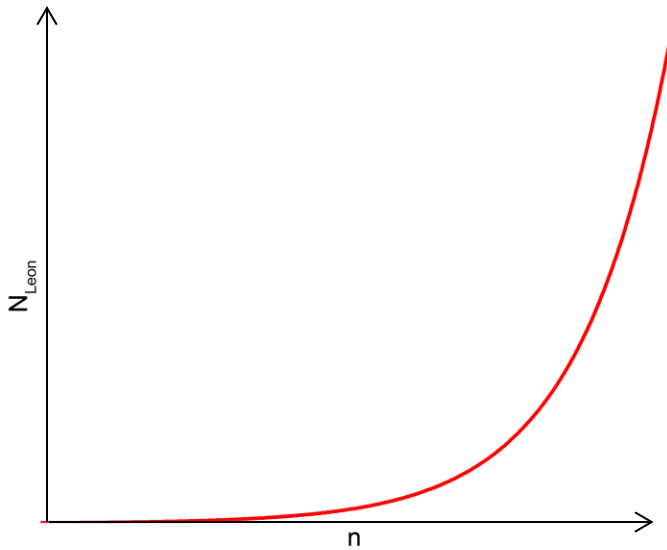
Primary	Secondary
Combustion releasing soot	Aggregates caused by lightning strikes

CATNIP

Not even once



Structure and the Fractal Sum



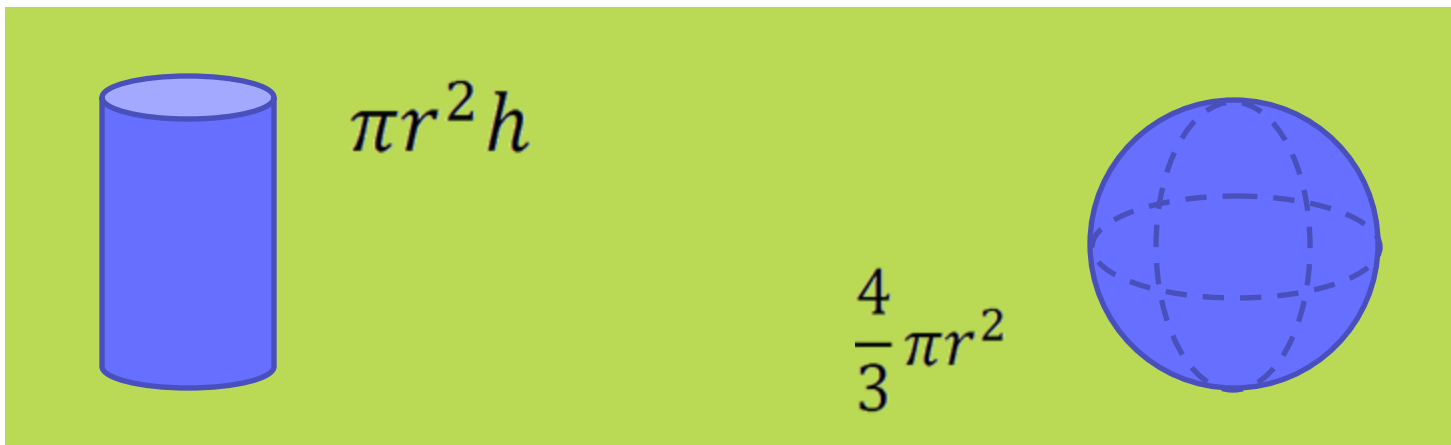
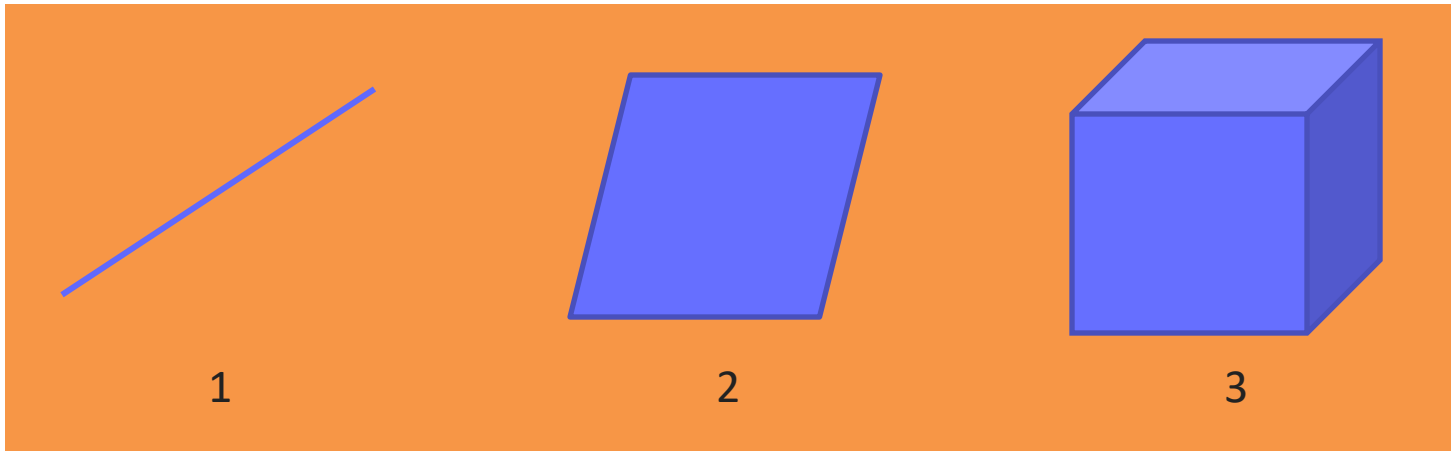
$$N_{Leon} = \sum_{i=0}^n 2^i - 1$$

$$\lim_{n \rightarrow \infty} N_{Leon} = \infty$$

$$N = k_0 \left(\frac{R_g}{a} \right)^{D_f}$$

R_g
 a
 k_0
 D_f

radius of gyration
 radius of single primary particle
 scaling prefactor
 fractal dimension



Probability to find another particle certain particle within distance r

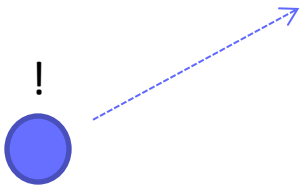
$$g(r) \sim r^{D_f - d} h\left(\frac{r}{R_g}\right)$$

Where $h(x)$ is our finite size cutoff function

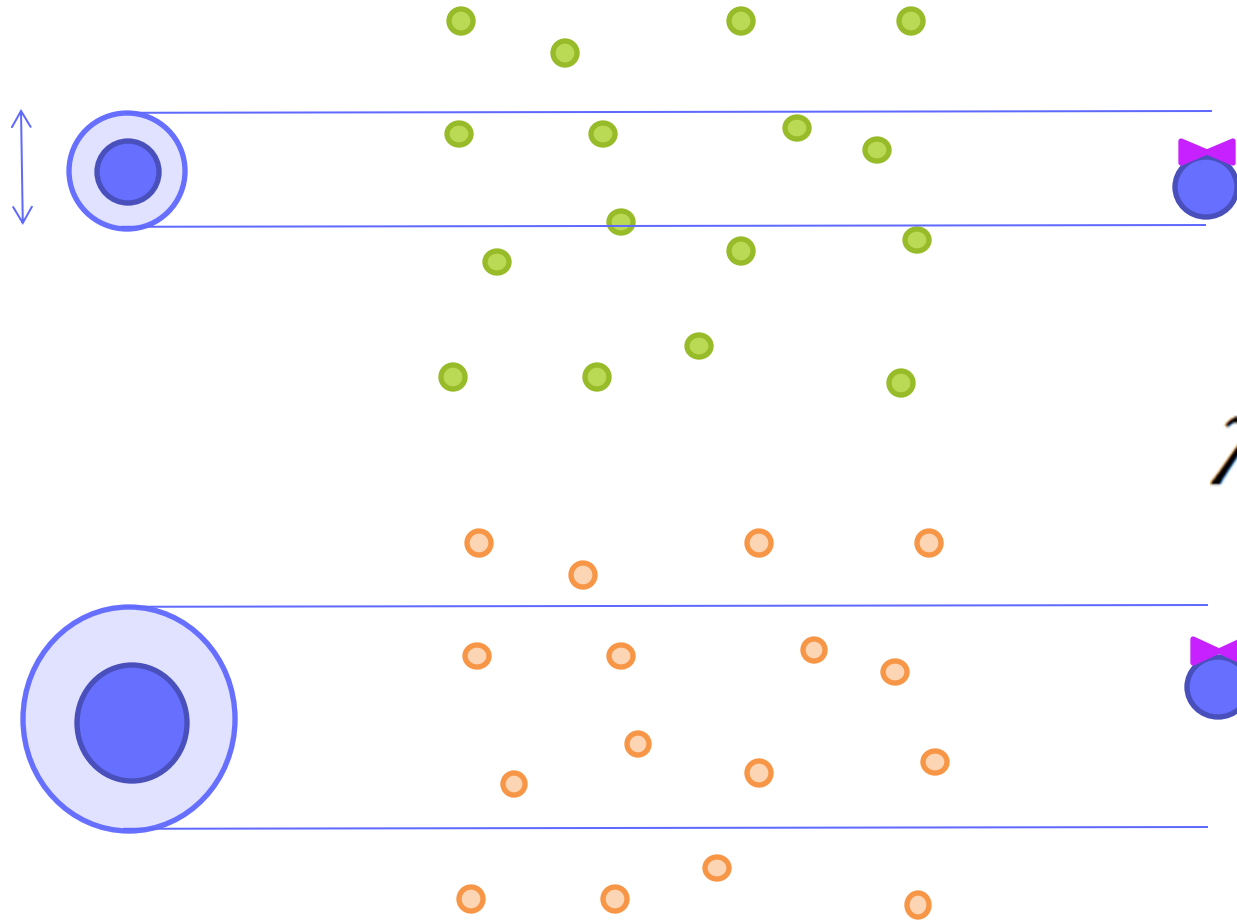
Which is bound by:

$$h(x) = e^{-x^\gamma} \begin{cases} x \ll 1 \rightarrow h(x) = 1 \\ x \gg 1 \rightarrow h(x) < g(r) \end{cases}$$

$$2 < \gamma < 2.5$$

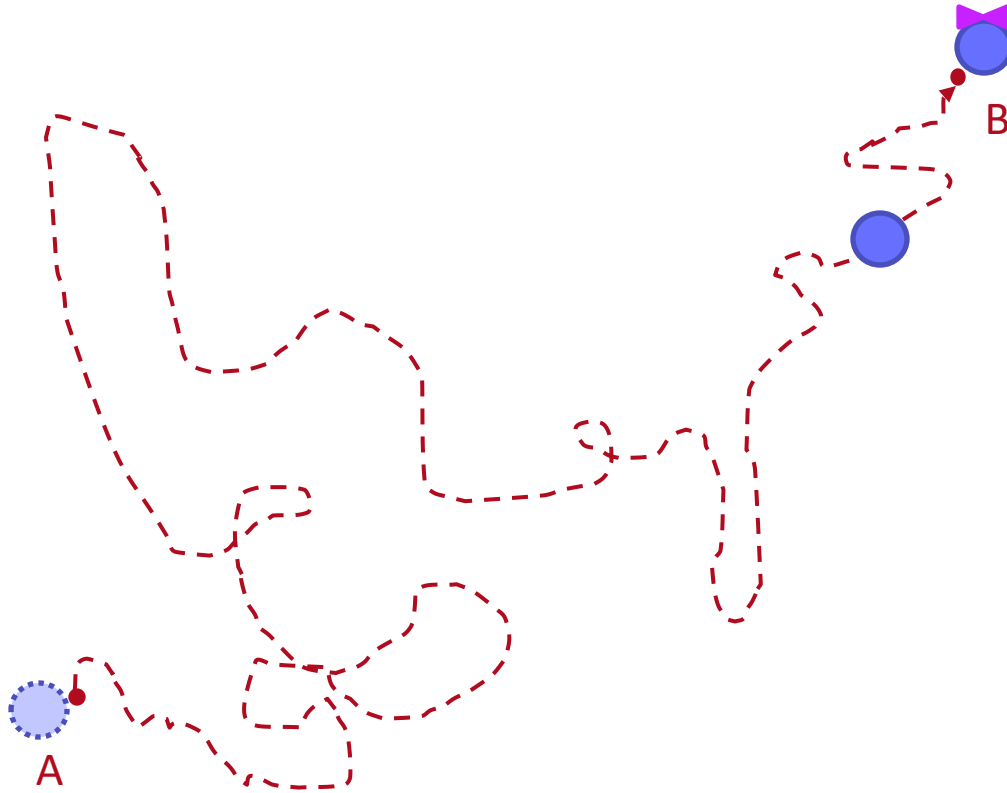


Mean Free Path with Increasing Mass



$$\lambda = \frac{2\mu}{\rho v}$$

Diffusion Limited Cluster Aggregation



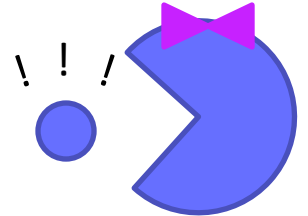
$$\lambda = \frac{2\mu}{\rho v}$$

$$\bar{v} = \sqrt{\frac{8k_B T}{\pi m}}$$

$$\lambda \gg d_p \quad \sqrt{d_p^5} = \sqrt{d_{p_0}^5} + \frac{10}{\pi} \sqrt{\frac{6k_B T}{\rho_p}} V t$$

Reaction Limited Cluster Aggregation

What if $\lambda \ll d_p$?

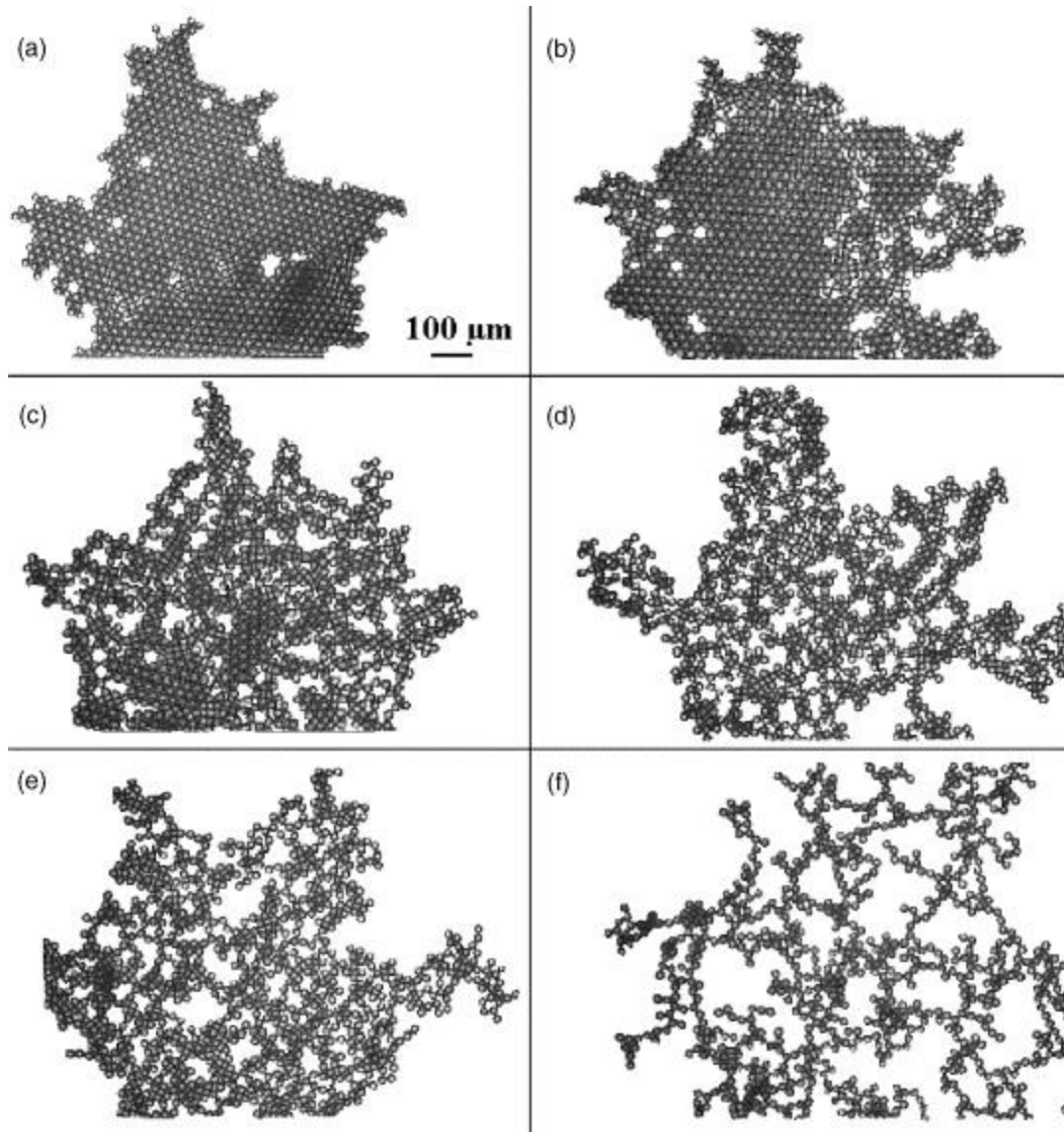


$$d_p = d_{p_0} + \frac{2k_s M_{W_p} C t}{a}$$

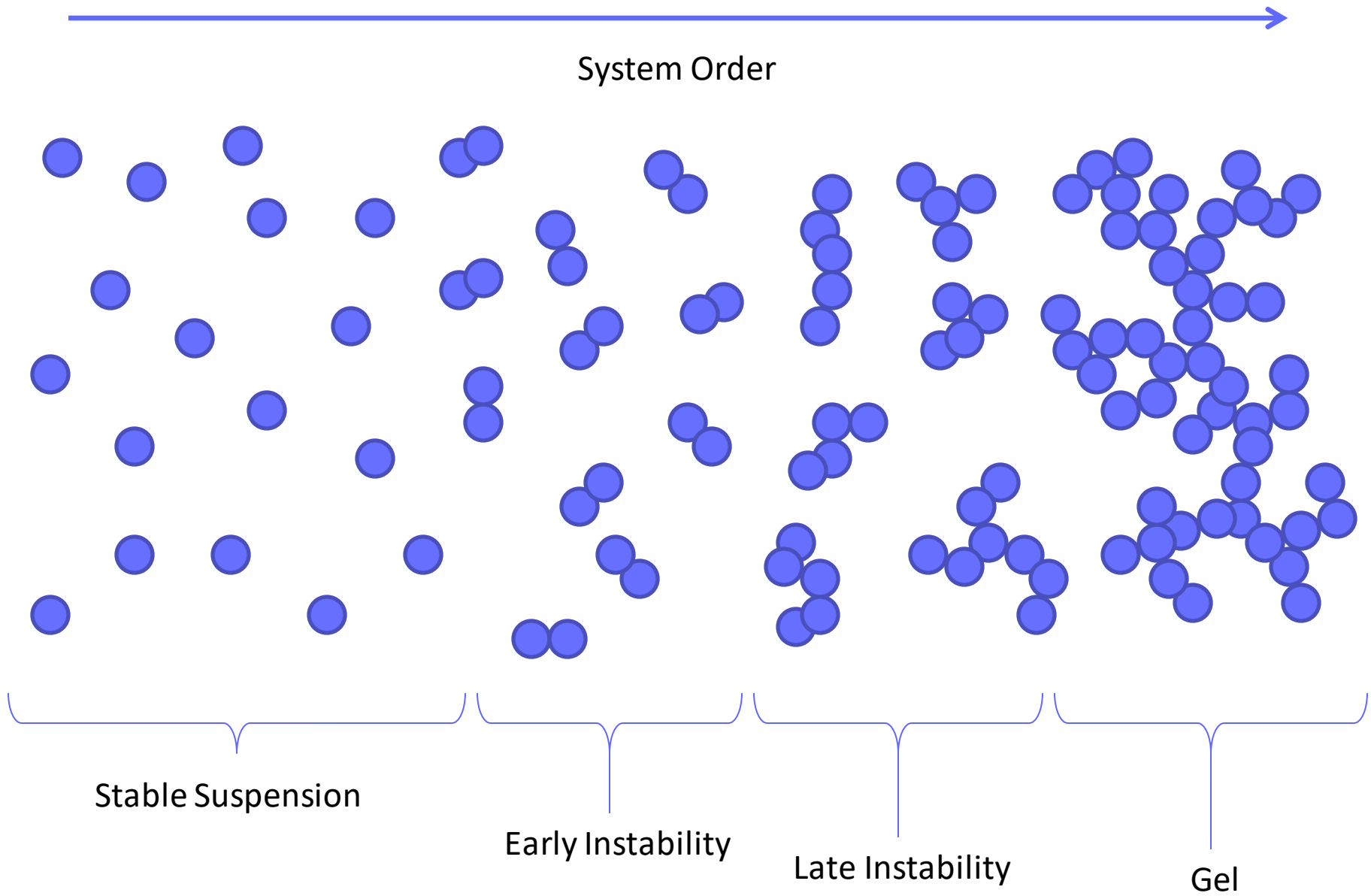
$$C = C_0 e^{-kt}$$

Commonly found in colloids, but has never been observed in aerosols.

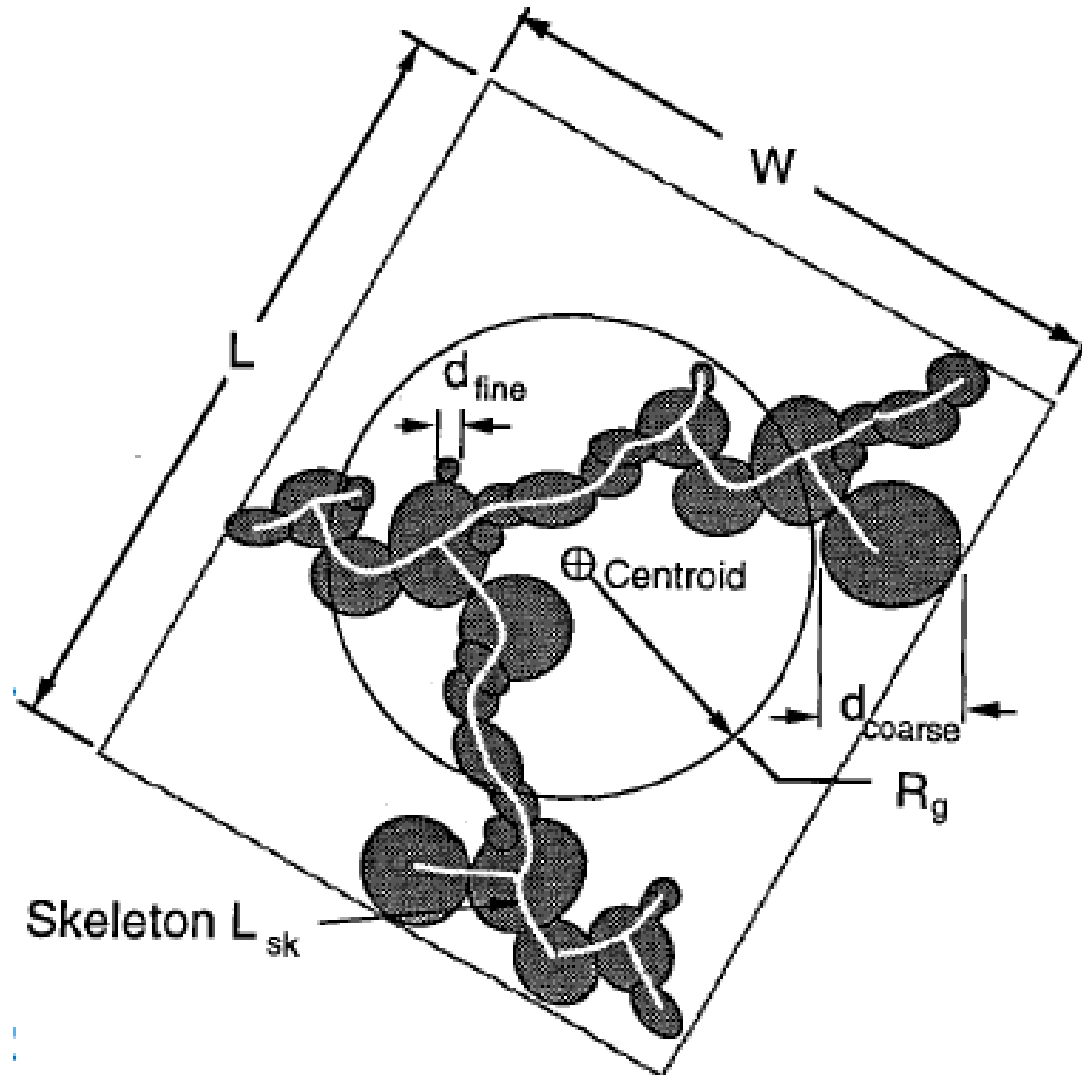
RLCA vs. DLCA



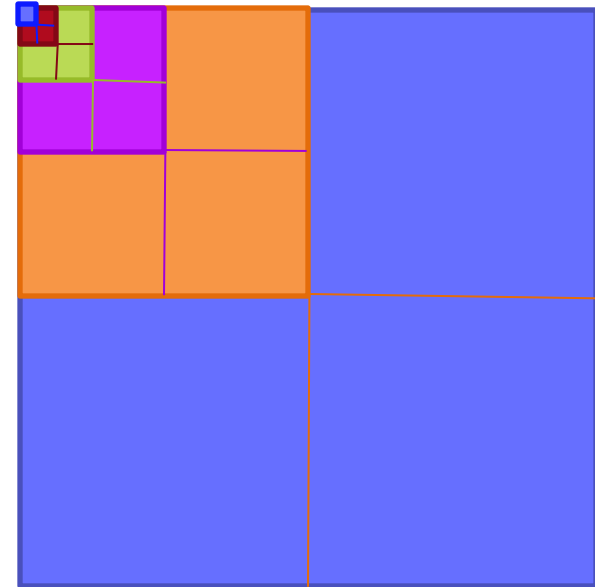
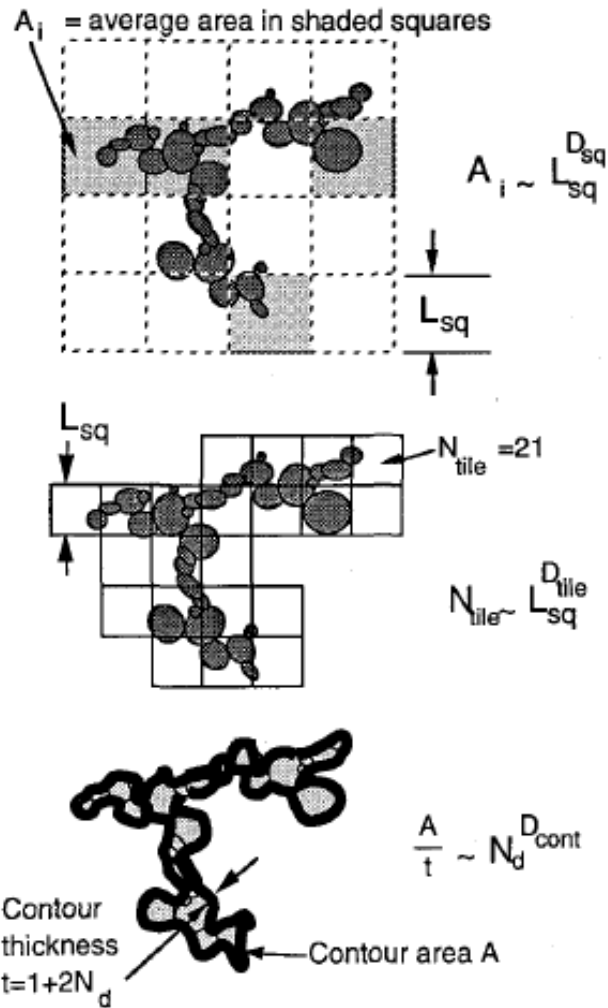
The Size Threshold



Characterizing with Non-Uniform Particles



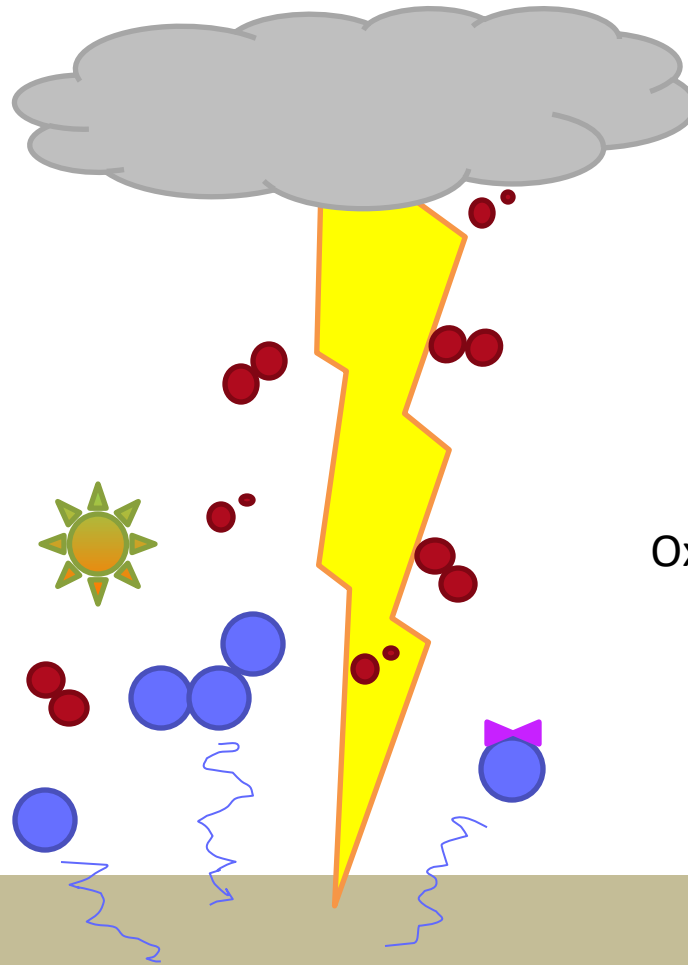
Tile Estimation



Smaller and smaller
Boxes estimate outline
Of the aggregate

Particle Aggregates and Ball Lightning

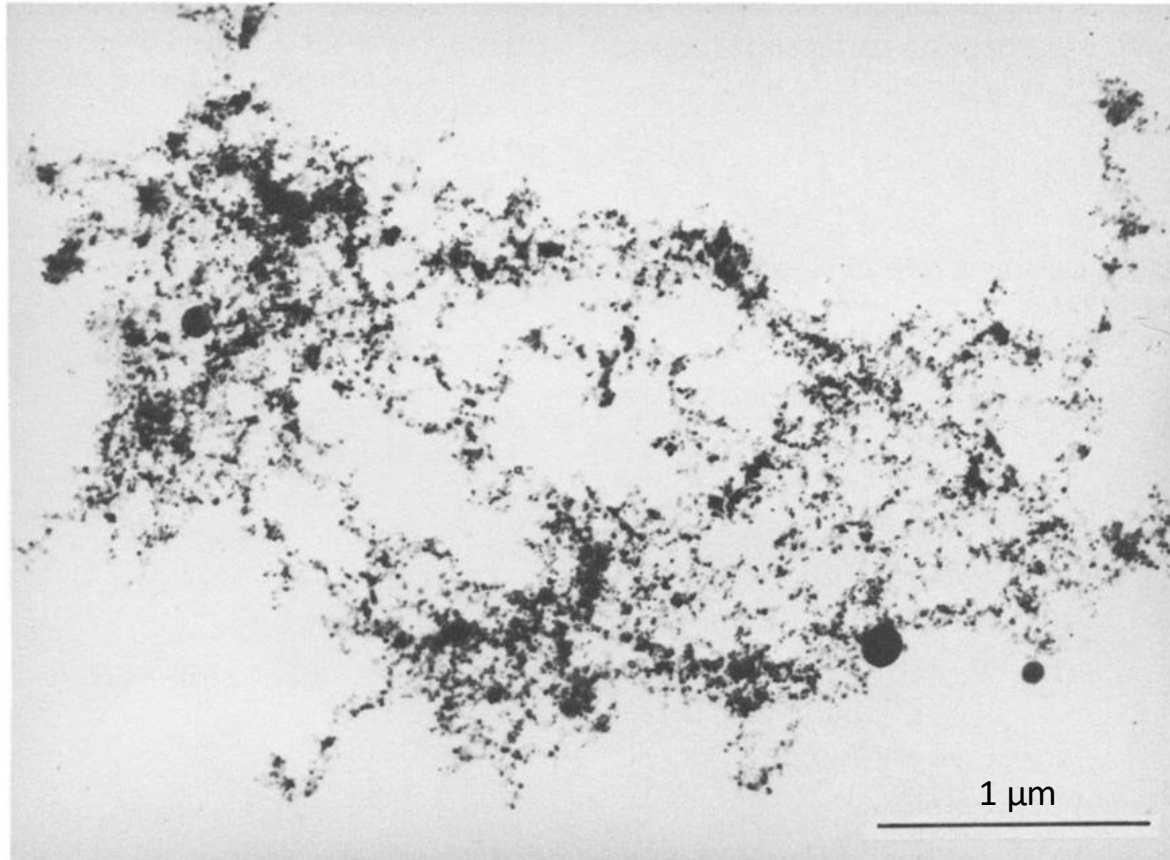
In 1987, Smirnov calculated from physical data from ball lightning occurrences, that particles may be the cause.



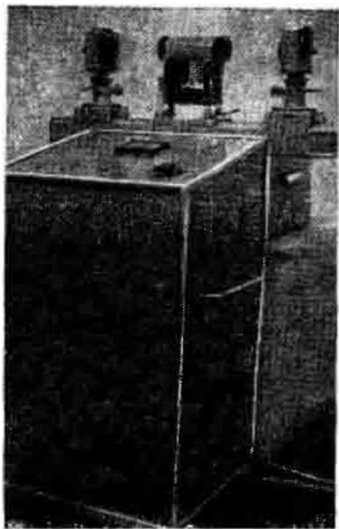
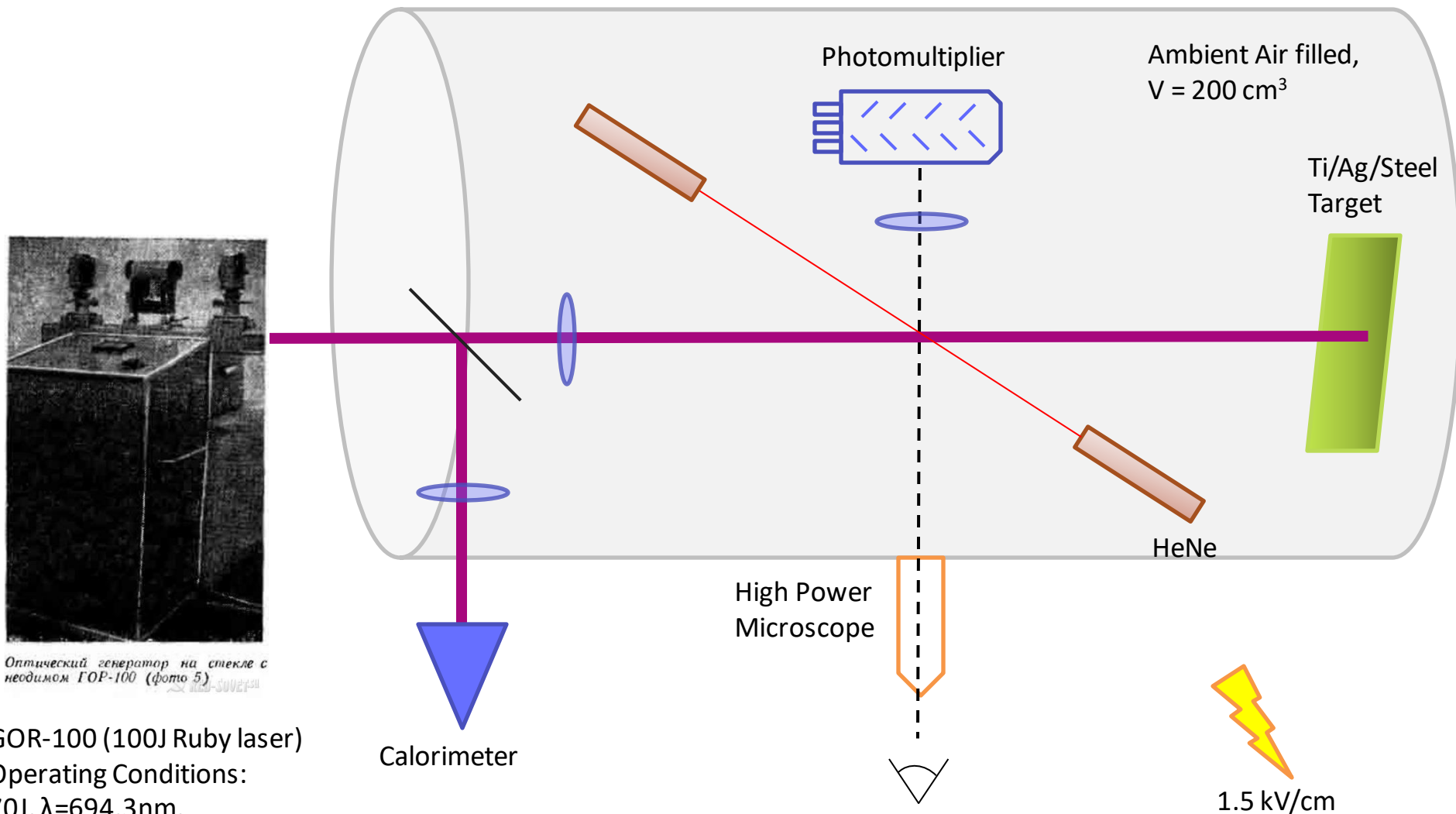
Oxidizing Aggregates

Silicon?

Aggregates in Electric Fields Aerosol to Aerogel



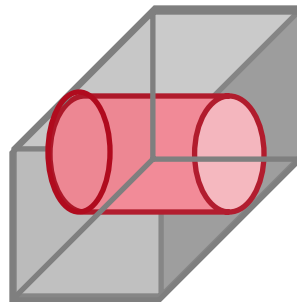
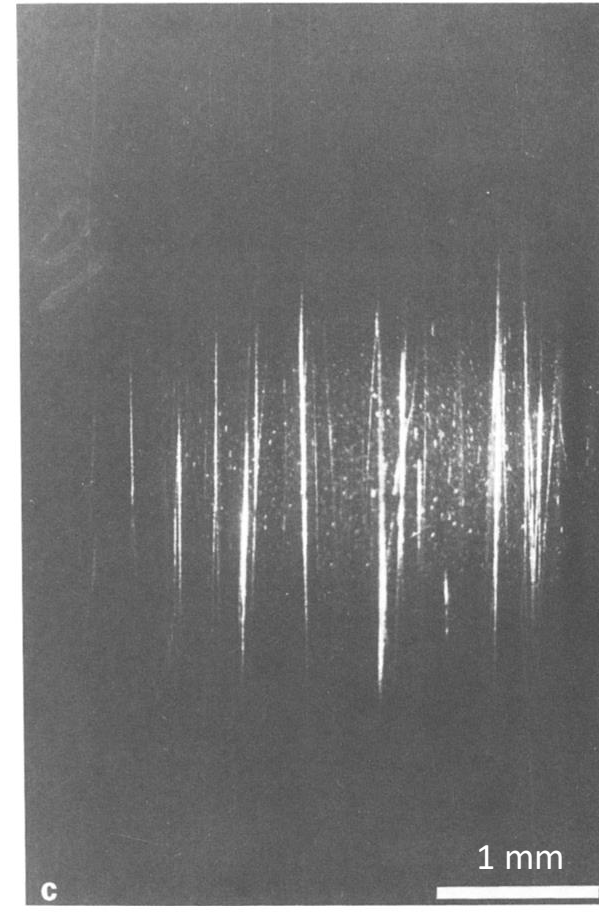
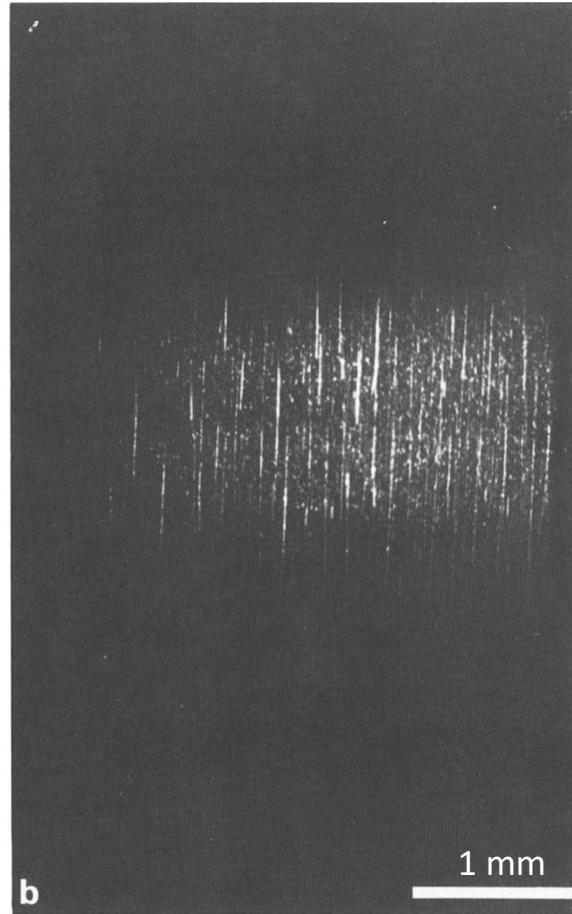
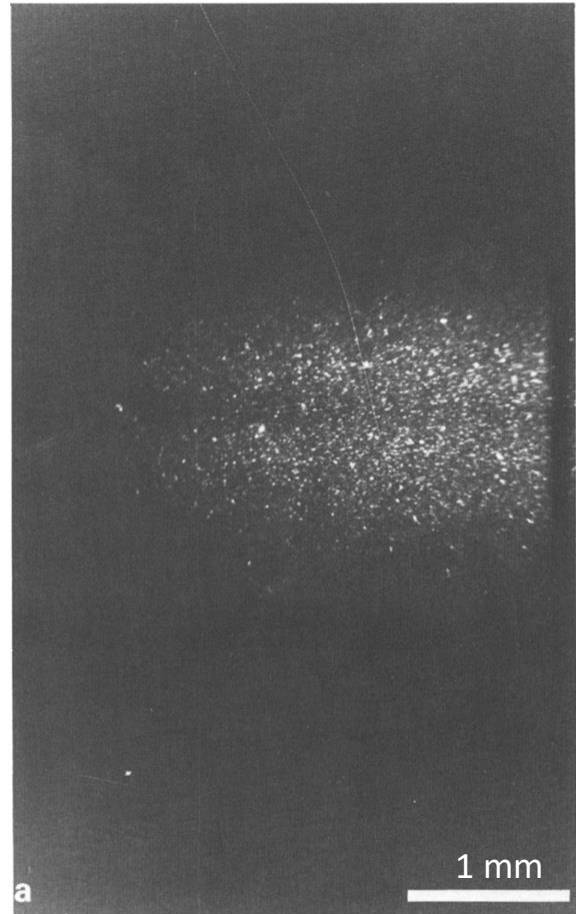
Experimental Setup



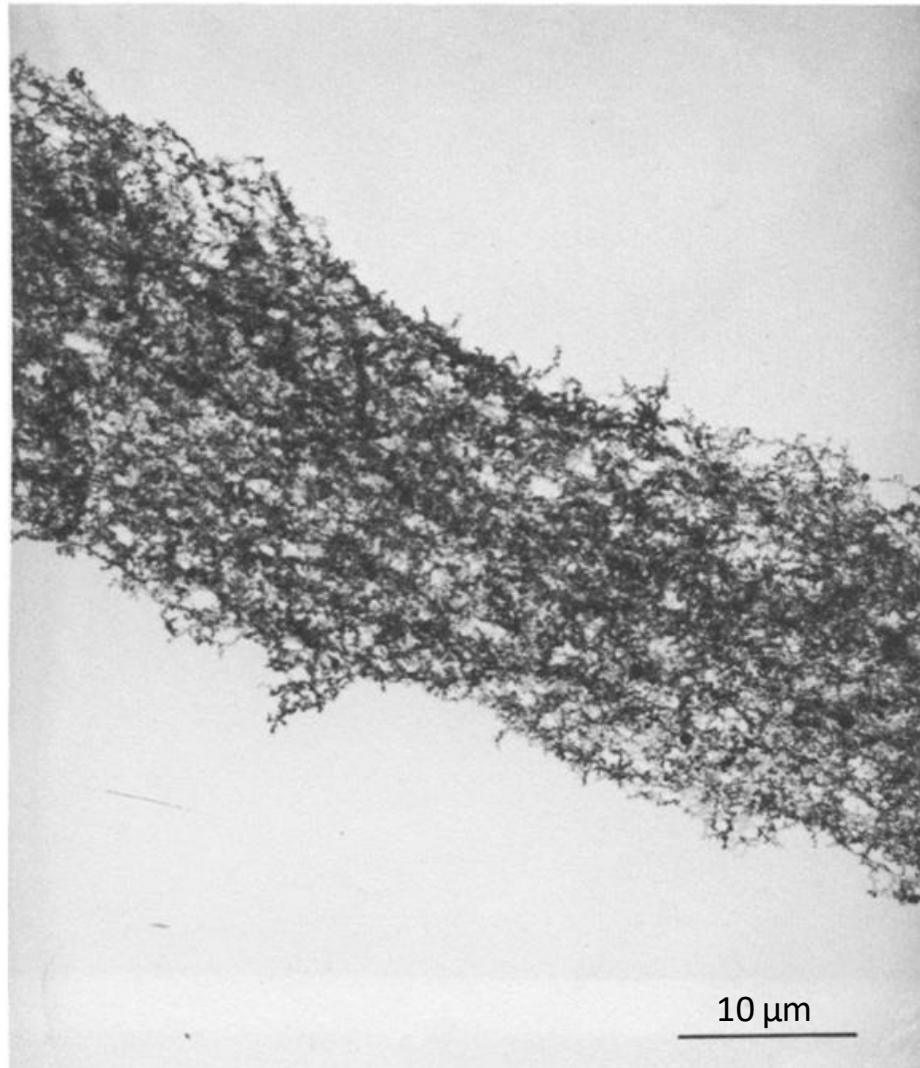
Оптический генератор на стекле с неодимом ГОР-100 (фото 5)

GOR-100 (100J Ruby laser)
Operating Conditions:
70J, $\lambda=694.3\text{nm}$,
Pulse Length $\tau=.001\text{s}$

Fiber Formation



Fibers Up Close



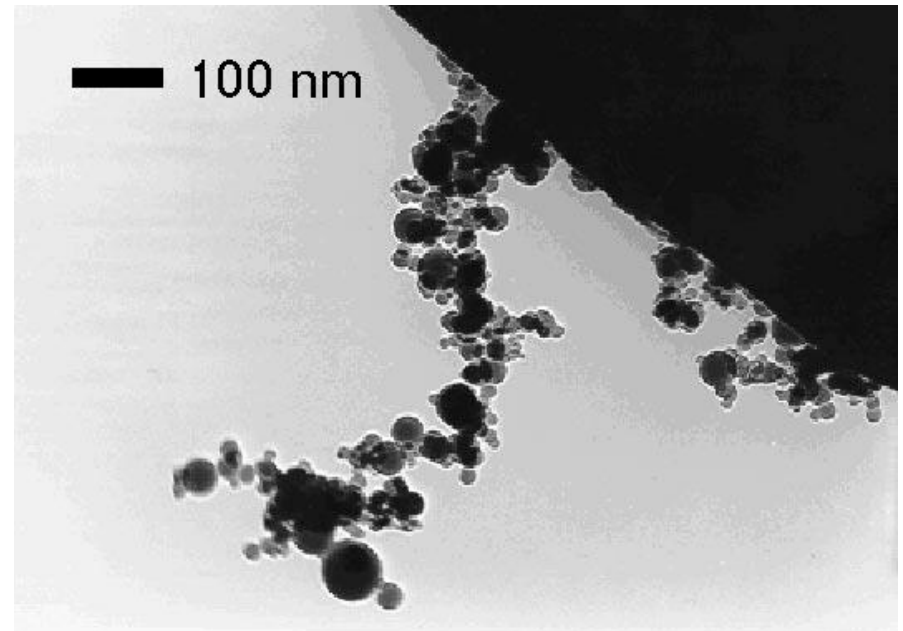
Oxidation of Networks

Based on Soviet experiment producing short lived ball lightning from carbonaceous loam (1977) – paper no longer available

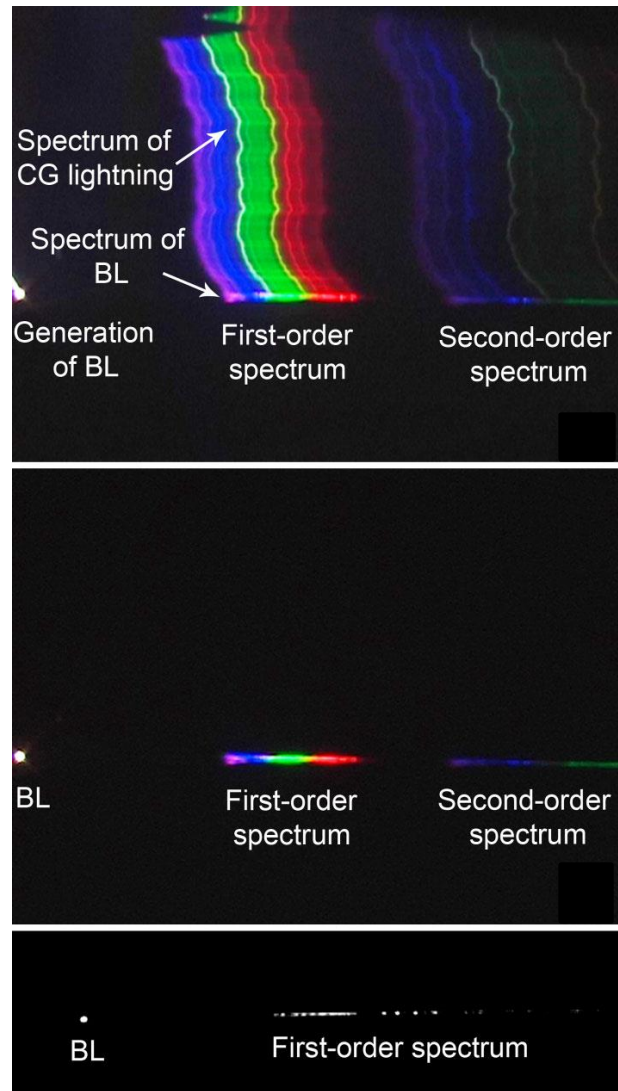
Did not match lifetime of observed

Created models based on Si oxidation, as suggested by Smirnov (1987)

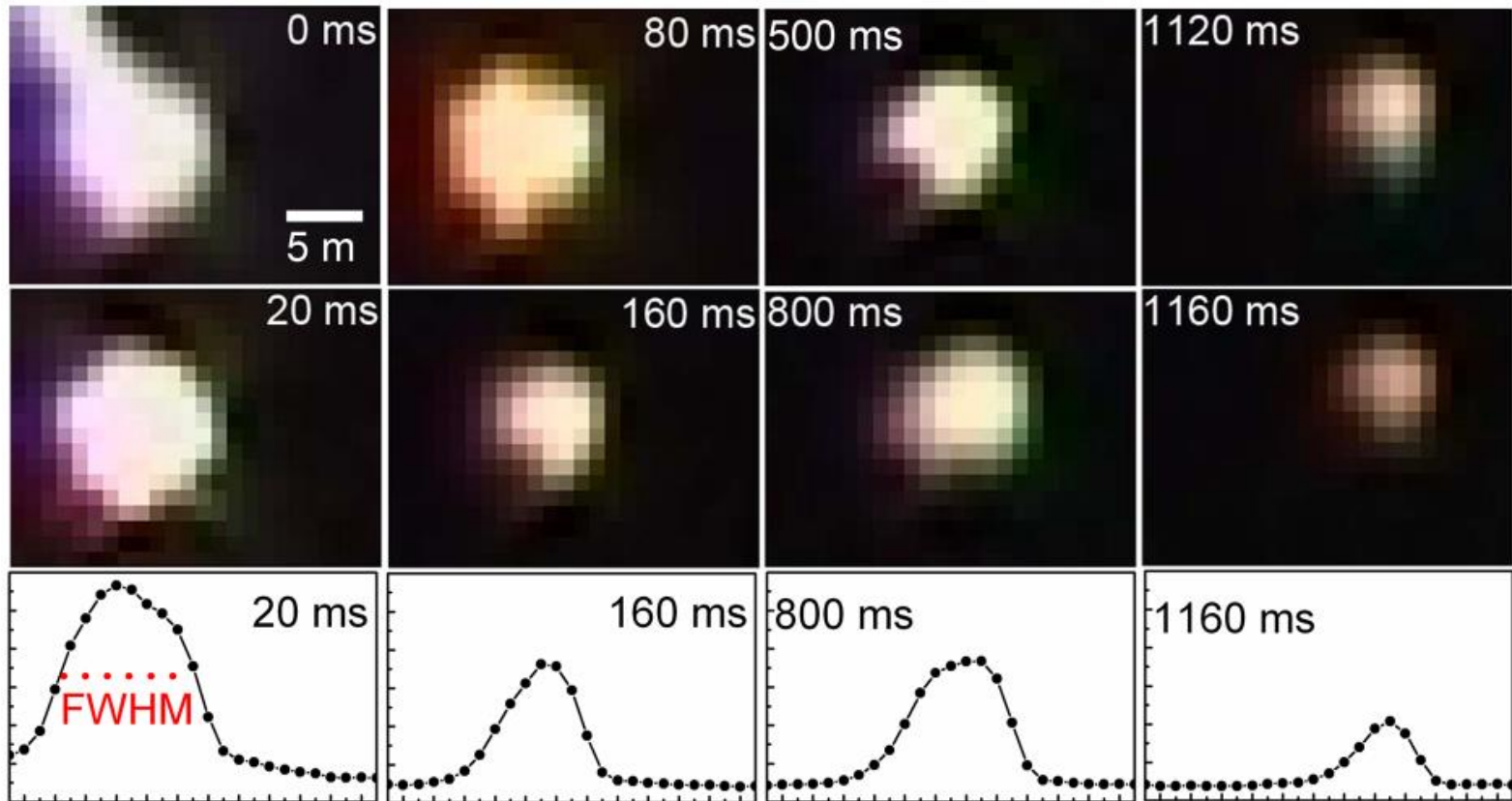
Used cooling techniques found in industrial processes



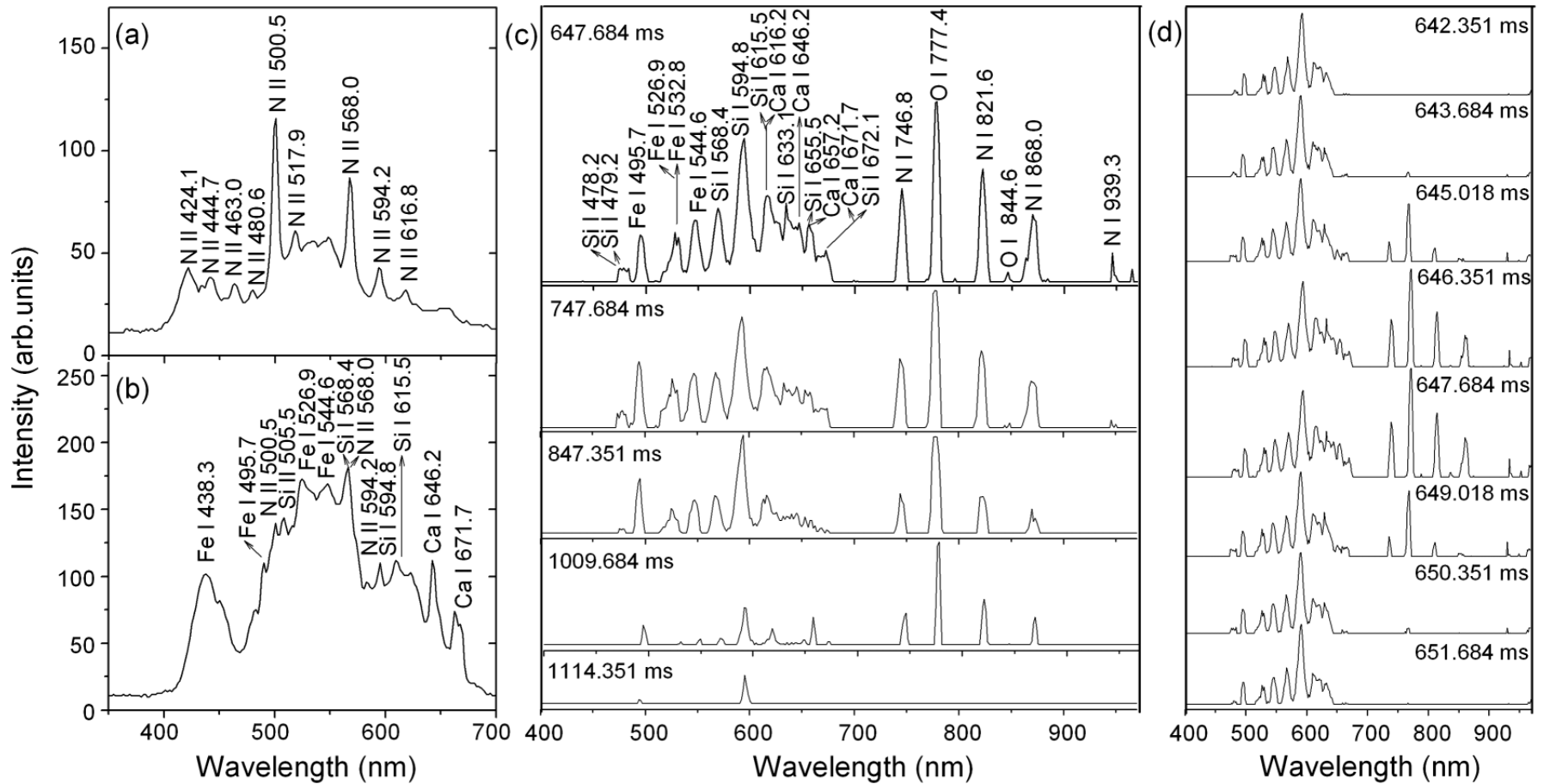
Observation with Modern Techniques



Zoom, Enhance



Spectral Analysis



Iron, Silicon, and Calcium all detected in the emission spectra

Can Ball Lightning Be Traced to Aggregates?

Known

Ball lightning due to metal oxidation

Fractal aggregation of particles occurs in high electric fields, to gel level of structure

Metal emission spectra observed in real occurrence

Unknown

The role of structure in aggregate

The role of size of structure

Possible changes in light scattering due to fractal aggregates

Ratios of metal atoms to carbon atoms in ejected particulate matter

Duration of charge field required for sufficient aggregation

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Dr. Claire Curry

Dr. Henry Kanarek

Oklahoma State University

Department of Chemistry

My gracious audience

The illustrious Leon

Structure	$R_g^2 =$	Parameters
Gaussian Coil	$\frac{Nb^2}{6}$	Degree of polymerization N Statistical segment length b
Gaussian Star	$\frac{3f - 2 N_{arm}b^2}{f} \frac{1}{6}$	Arm degree of polymerization N_{arm} Number of arms f Statistical segment length b
Gaussian Ring	$\frac{Nb^2}{12}$	Statistical segment length b Degree of polymerization N
Solid Sphere	$\frac{3}{5}R^2$	Sphere radius R
Solid Ellipsoid	$\frac{1}{5}(R_1^2 + R_2^2 + R_3^2)$	Ellipsoid principal radii R_n
Thin Rod	$\frac{1}{12}L^2$	Rod Length L
Cylinder	$\frac{1}{12}L^2 + \frac{1}{2}r^2$	Cylinder radius r Length L
Thin Disk	$\frac{1}{2}r^2$	Disk radius r

Reynolds Number

$$Re = \frac{ua}{\nu}$$

Stokes Number

$$Stk = \frac{2a^2u}{9\nu L}$$

Knudsen Numbers

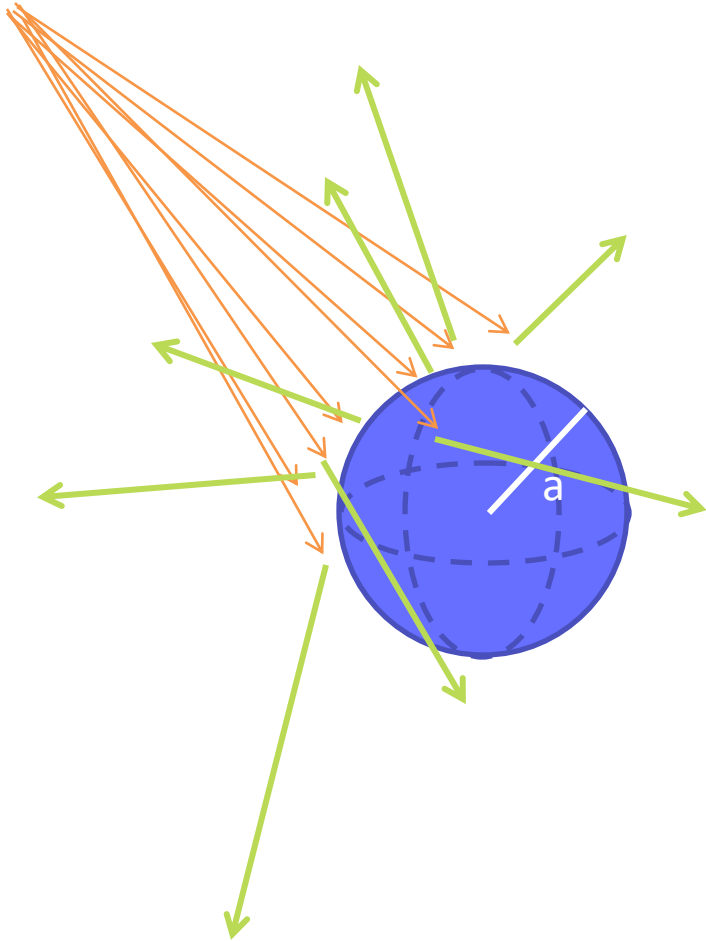
$$Kn = \frac{\lambda}{a}$$

$$Kn = \frac{2D_f}{\sqrt{\frac{8kT}{\pi m}} a}$$

Peclet Number

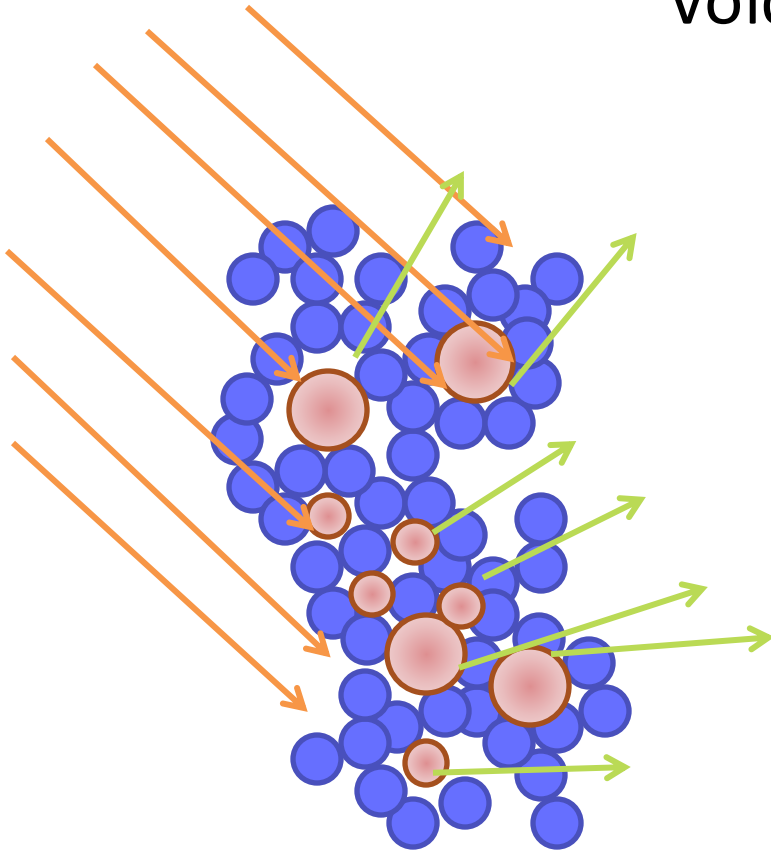
$$Pe = \frac{2\Lambda}{\sqrt{\frac{8kT}{\pi m}} a}$$

Mie Scattering



$$Mie = \frac{2\pi\lambda_w}{a}$$

Void Optics



$$n_{void}(a) = \frac{3 - D_f}{R_g^{3-D_f}} a^{2-D_f}$$

$$V_{void}(a) = \frac{4\pi(6 - D_f)}{3(3 - D_f)} a^3$$

$$\sigma_{abs} = \frac{6\pi \text{Im} \left(\frac{m^2 - 1}{m^2 + 2} \right)}{\lambda_w \rho}$$